

Please write clearly in	block capitals.		
Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

# GCSE MATHEMATICS

H

Higher Tier

Paper 1 Non-Calculator

Tuesday 21 May 2019

Morning

Time allowed: 1 hour 30 minutes

### **Materials**

For this paper you must have:

· mathematical instruments



You must **not** use a calculator.

#### Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

#### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

#### **Advice**

In all calculations, show clearly how you work out your answer.

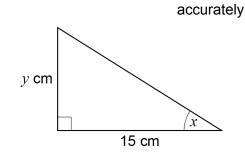


For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
TOTAL	

## Answer all questions in the spaces provided

**1** Here are two right-angled triangles.

6 cm x 10 cm



Circle the value of *y*.

[1 mark]

- 11
- 7.5
- 9
- 4

Not drawn

2 Work out the value of  $\left(1\frac{2}{3}\right)^2$ 

Circle your answer.

[1 mark]

- $1\frac{4}{9}$
- $3\frac{1}{3}$
- $2\frac{4}{9}$
- $2\frac{7}{9}$
- Work out the arc length, in metres, of a semicircle of radius 6 metres. Circle your answer.

[1 mark]

- 3π
- 6π
- $12\pi$
- 18π

4	Circle the fraction that is equivalent to	4.625

[1 mark]

$$\frac{39}{8}$$

$$\frac{37}{8}$$

$$\frac{17}{4}$$

5	(a)	Write	0.00097	in standard form.
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[1 mark]

Answer	

**5 (b)** Work out 
$$\frac{3 \times 10^5}{4 \times 10^3}$$

Give your answer as a	an ordinary numbei
-----------------------	--------------------

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	_		ч	ır	v

Answer \_\_\_\_\_

7

**6** Anna plays a game with an ordinary, fair dice.

If she rolls 1 she wins.

If she rolls 2 or 3 she loses.

If she rolls 4, 5 or 6 she rolls again.

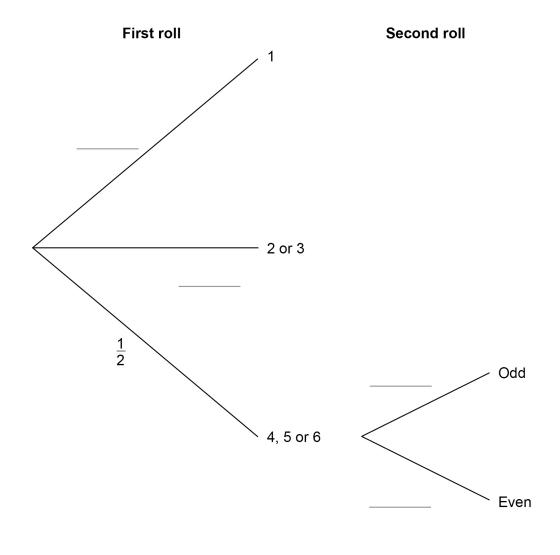
When she has to roll again,

if she rolls an odd number she wins

if she rolls an even number she loses.

**6** (a) Complete the tree diagram with the four missing probabilities.

[2 marks]





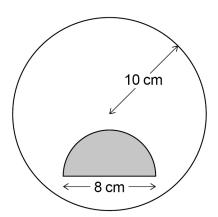
_				οι
6	(b)	Is Anna more likely to win or to lose?		
		You <b>must</b> work out the probability that she wins.		
			[4 marks]	
		Turn over for the next question		
		Turn over for the next question		

Do not write outside the box

7	Three friends arrive at a party.	
	Their arrival increases the number of people at the party by 20%	
	In total, how many people are now at the party?	[2 marks]
	Answer	_
8	Work out the value of $(3^{12} \div 3^5) \div (3^2 \times 3)$	[3 marks]
		[o marko]
	Answer	_



**9** A shaded semicircle is inside a circle as shown.



Not drawn accurately

The radius of the circle is 10 cm

The diameter of the semicircle is 8 cm

low many times bigger is the unshaded area than the shaded area?	[4 marks]

Turn over for the next question

Answer \_\_\_\_\_

9



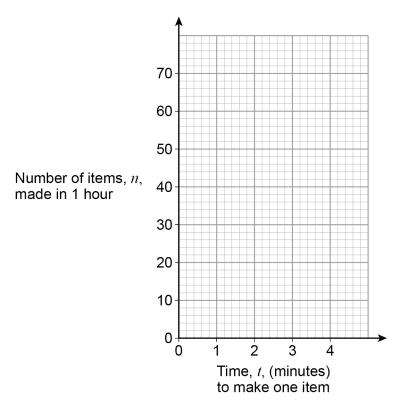
The number of items, n, made in 1 hour by a machine is given by  $n = \frac{60}{t}$ 

t is the time in minutes the machine takes to make one item.

The value of t changes for different types of item.

10 (a) On the grid below, draw the graph of  $n = \frac{60}{t}$  for values of t from 1 to 4

[2 marks]



**10 (b)** The machine takes 3 minutes 30 seconds to make one item.

**Use your graph** to estimate the value of n.

[2 marks]

Answer

11	Ed and Fay shared £330 in the ratio	7:4
----	-------------------------------------	-----

Ed gives Fay some of his money.

Fay now has the same amount as Ed.

How much does Ed give Fay?

[3 marks]

Answer £

The next term of a sequence is made by adding the previous two terms.

Which of these sequences follows this rule? Circle your answer.

[1 mark]

-9 2 -7 -5 -12

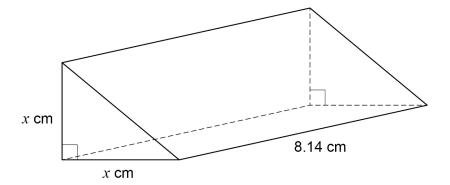
-3 5 -2 3 1

0 -3 -3 0 -3

-1 -1 -2 -3 1

8

The triangular cross section of a prism is an isosceles right-angled triangle.



The volume of the prism is  $102~\mathrm{cm}^3$ 

Use approximations to estimate the value of x.

Answer

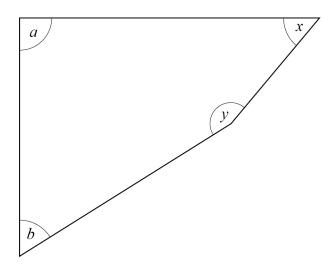
You **must** show your working.



[3 marks]

Do not write outside the box

14 Here is a quadrilateral.



Not drawn accurately

 $a = 90^{\circ}$  and a : b = 5 : 3

x: y = 1:3

Show that b = x

[3 marks]

		Т

6



Do not write outside the box

Here is some information about the test marks of 120 students.

Mark, m	0 < <i>m</i> ≤ 10	10 < <i>m</i> ≤ 20	20 < <i>m</i> ≤ 30	30 < <i>m</i> ≤ 40	40 < <i>m</i> ≤ 50
Frequency	20	28	40	20	12

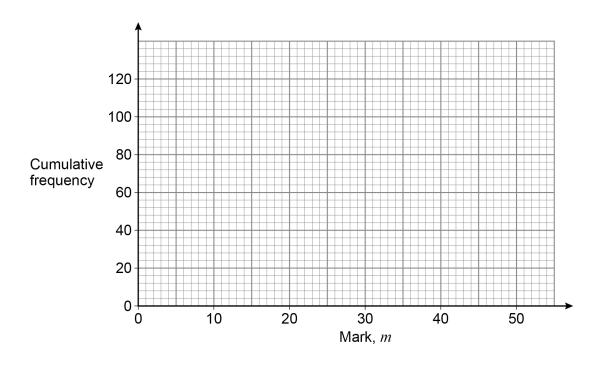
**15** (a) Complete the cumulative frequency table.

[1 mark]

Mark, m	<i>m</i> ≤ 10	<i>m</i> ≤ 20	<i>m</i> ≤ 30	<i>m</i> ≤ 40	<i>m</i> ≤ 50
Cumulative frequency	20	48			

**15 (b)** Draw a cumulative frequency graph.

[2 marks]



Students who scored 15 marks or fewer take another test.	
Use your graph to estimate how many students take another test.	[2 marks]
Answer	_
Simplify fully $\frac{4x - 8x^2}{12x - 6}$	[3 marks]
Answer	
Turn over for the next question	
	Use your graph to estimate how many students take another test.  Answer  Simplify fully $\frac{4x-8x^2}{12x-6}$ Answer

8



- 17 Toby is forming and solving equations.
- 17 (a)

The product of half of a number and three more than the number is the same as the square of the number

Toby uses *y* to represent the number.

Write an equation that Toby could form.

[2 marks]

Answer

**17 (b)** Toby forms another equation.

$$x = \frac{9}{8x}$$

He wants to work out the values of x.

Here is his working.

$$x = \frac{9}{8x}$$

$$8x^2 = 9$$

$$8x = 3$$
 or  $8x = -3$ 

$$x = \frac{3}{8}$$
 or  $x = -\frac{3}{8}$ 

What error has he made in his working?

[1 mark]

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18 Here is an identity.

$$x^2 - y^2 \equiv (x + y)(x - y)$$

18 (a) Use the identity to work out the value of  $193^2 - 7^2$ You **must** show your working.

[2 marks]

Answer \_\_\_\_\_

**18 (b)** Factorise  $100a^2 - 81b^2$ 

[1 mark]

Answer \_\_\_\_\_

19 Circle the fraction that is equivalent to 0.1

[1 mark]

 $\frac{1}{9}$ 

 $\frac{1}{99}$ 

 $\frac{1}{10}$ 

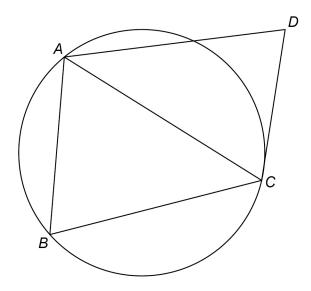
11 100

7

A, B and C are points on a circle.

CD is a tangent.

Not drawn accurately



20 (a) Assume that triangle ABC is isosceles with AC = BC

Prove that AB is parallel to DC.	[4 marks]
	_

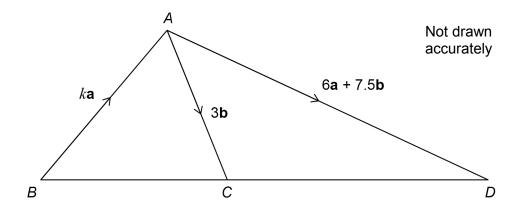


			'
20	(b)	In fact, triangle ABC is equilateral.	
		Tick the <b>two</b> boxes for the statements that <b>must</b> be correct.  [1 mark	1
		[· ···· <del>s</del> ····	•
		AB is parallel to DC	
		AC bisects angle BCD	
		AC bisects angle BAD	
21		Solve the simultaneous equations	
		2x + 3y = 5p	
		y = 2x + p	
		where $p$ is a constant.	
		where $p$ is a constant. Give your answers in terms of $p$ in their simplest form.	_
			]
		Give your answers in terms of $p$ in their simplest form.	<b>1</b>
		Give your answers in terms of $p$ in their simplest form.	] - -
		Give your answers in terms of $p$ in their simplest form.	<b>1</b>
		Give your answers in terms of $p$ in their simplest form.	] - - -
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		Give your answers in terms of $p$ in their simplest form.	<b>1</b>
		Give your answers in terms of $p$ in their simplest form.	] - - - - - -
		Give your answers in terms of $p$ in their simplest form.	] - - - - - -



22 ABC and ACD are triangles.

k is a constant.



22 (a) Show that  $\overrightarrow{CD} = 6a + 4.5b$ 

[1 mark]

22	(h)	BCD is a straight line

Work out the value of k.

You **must** show your working.

[3 marks]

Answer

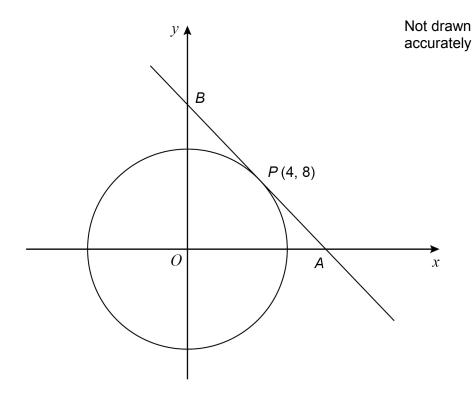
	19			
23	Simplify $8^4 \div 32^{\frac{2}{5}}$ Give your answer in the form $2^m$ where	m is an integer.	[3 marks]	Do not write outside the box
	Answer			
24	$f(x) = \sin(x - 90^{\circ})$ Circle the value of $f(0^{\circ})$		[4 mark]	
	1 0	$-\frac{1}{2}$	[ <b>1 mark]</b> –1	
	Turn over for the n	ext question		



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**25** P (4, 8) is a point on a circle, centre O.

The tangent at P intersects the axes at points A and B.



25 (a) Show that the gradient of the tangent is  $-\frac{1}{2}$ 

[2 marks]

	21	
Work out the length $AB$ . Give your answer in the form $a\sqrt{5}$ You <b>must</b> show your working.	where $a$ is an integer.	[/ marks]
		[4 marks]
Answer	units	

Turn over for the next question



26	The turning point of the graph $y = (x + a)^2 + b$ has x-coordinate $-2$ (3, 1) is another point on the graph.	
	Work out the <i>y</i> -coordinate of the turning point.	[3 marks]
	Answer	



			Do not write outside the
27	Angle <i>x</i> is acute.		box
	$\cos x = \sin 60^\circ \times \tan 30^\circ$		
	Work out the size of angle $x$ .		
	You <b>must</b> show your working.		
		[3 marks]	
	Answer	degrees	
	END OF QUESTIONS		

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