## AQA

Please write clearly in block capitals.

Centre number


Candidate number


Surname
Forename(s)
Candidate signature $\qquad$

## GCSE

MATHEMATICS
Higher Tier

## Paper 1 Non-Calculator

Tuesday 21 May 2019
Morning
Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- mathematical instruments

You must not use a calculator.


## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $2-3$ |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| TOTAL |  |

- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## Advice

In all calculations, show clearly how you work out your answer.
Answer all questions in the spaces provided

1 Here are two right-angled triangles.
Not drawn accurately


Circle the value of $y$.
11
7.5
9
4

2 Work out the value of $\left(1 \frac{2}{3}\right)^{2}$
Circle your answer.
$1 \frac{4}{9}$
$3 \frac{1}{3}$
$2 \frac{4}{9}$
$2 \frac{7}{9}$

3 Work out the arc length, in metres, of a semicircle of radius 6 metres. Circle your answer.
$3 \pi$
$6 \pi$
$12 \pi$
$18 \pi$

$6 \quad$ Anna plays a game with an ordinary, fair dice.
If she rolls 1 she wins.
If she rolls 2 or 3 she loses.
If she rolls 4,5 or 6 she rolls again.
When she has to roll again,
if she rolls an odd number she wins
if she rolls an even number she loses.

6 (a) Complete the tree diagram with the four missing probabilities.


6 (b) Is Anna more likely to win or to lose?
You must work out the probability that she wins.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$

Turn over for the next question
$7 \quad$ Three friends arrive at a party.
Their arrival increases the number of people at the party by 20\% In total, how many people are now at the party?
$\qquad$

Answer $\qquad$
$8 \quad$ Work out the value of $\quad\left(3^{12} \div 3^{5}\right) \div\left(3^{2} \times 3\right)$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

9 A shaded semicircle is inside a circle as shown.


Not drawn accurately

The radius of the circle is 10 cm
The diameter of the semicircle is 8 cm
How many times bigger is the unshaded area than the shaded area?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

10 The number of items, $n$, made in 1 hour by a machine is given by $n=\frac{60}{t}$ $t$ is the time in minutes the machine takes to make one item. The value of $t$ changes for different types of item.

10 (a) On the grid below, draw the graph of $n=\frac{60}{t}$ for values of $t$ from 1 to 4


10 (b) The machine takes 3 minutes 30 seconds to make one item.

$$
\text { Use your graph to estimate the value of } n \text {. }
$$

Answer $\qquad$

11 Ed and Fay shared $£ 330$ in the ratio $7: 4$
Ed gives Fay some of his money.
Fay now has the same amount as Ed.
How much does Ed give Fay?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £

12 The next term of a sequence is made by adding the previous two terms.
Which of these sequences follows this rule?
Circle your answer.

$$
\begin{array}{lllll}
-9 & 2 & -7 & -5 & -12
\end{array}
$$

$$
\begin{array}{lllll}
-3 & 5 & -2 & 3 & 1
\end{array}
$$

$\begin{array}{lllll}0 & -3 & -3 & 0 & -3\end{array}$

$$
\begin{array}{lllll}
-1 & -1 & -2 & -3 & 1
\end{array}
$$

13 The triangular cross section of a prism is an isosceles right-angled triangle.


The volume of the prism is $102 \mathrm{~cm}^{3}$
Use approximations to estimate the value of $x$.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

14 Here is a quadrilateral.
Not drawn
 accurately
$a=90^{\circ}$ and $a: b=5: 3$
$x: y=1: 3$
Show that $b=x$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

15 Here is some information about the test marks of 120 students.

| Mark, $\boldsymbol{m}$ | $0<m \leqslant 10$ | $10<m \leqslant 20$ | $20<m \leqslant 30$ | $30<m \leqslant 40$ | $40<m \leqslant 50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 20 | 28 | 40 | 20 | 12 |

15 (a) Complete the cumulative frequency table.

| Mark, $\boldsymbol{m}$ | $m \leqslant 10$ | $m \leqslant 20$ | $m \leqslant 30$ | $m \leqslant 40$ | $m \leqslant 50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Cumulative <br> frequency | 20 | 48 |  |  |  |

15 (b) Draw a cumulative frequency graph.


15 (c) Students who scored 15 marks or fewer take another test.
Use your graph to estimate how many students take another test.
$\qquad$
$\qquad$

Answer $\qquad$

16 Simplify fully $\frac{4 x-8 x^{2}}{12 x-6}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

17 Toby is forming and solving equations.
17 (a)
The product of half of a number and three more than the number is the same as the square of the number

Toby uses $y$ to represent the number.
Write an equation that Toby could form.
$\qquad$
$\qquad$

Answer

17 (b) Toby forms another equation.

$$
x=\frac{9}{8 x}
$$

He wants to work out the values of $x$.
Here is his working.

$$
\begin{aligned}
x & =\frac{9}{8 x} \\
8 x^{2} & =9 \\
8 x & =3 \text { or } 8 x=-3 \\
x & =\frac{3}{8} \text { or } x=-\frac{3}{8}
\end{aligned}
$$

What error has he made in his working?
$\qquad$
$\qquad$
$\qquad$

18 Here is an identity.

$$
x^{2}-y^{2} \equiv(x+y)(x-y)
$$

18 (a) Use the identity to work out the value of $193^{2}-7^{2}$ You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

18 (b) Factorise $100 a^{2}-81 b^{2}$

## Answer

19 Circle the fraction that is equivalent to 0.1
$\frac{1}{9}$
$\frac{1}{99}$
$\frac{1}{10}$
$\frac{11}{100}$
$20 \quad A, B$ and $C$ are points on a circle.
$C D$ is a tangent.
Not drawn accurately

20 (a) Assume that triangle $A B C$ is isosceles with $A C=B C$ Prove that $A B$ is parallel to $D C$.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

20 (b) In fact, triangle $A B C$ is equilateral.
Tick the two boxes for the statements that must be correct.


21 Solve the simultaneous equations

$$
\begin{aligned}
2 x+3 y & =5 p \\
y & =2 x+p
\end{aligned}
$$

where $p$ is a constant.
Give your answers in terms of $p$ in their simplest form.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$x=$ $\qquad$ $y=$ $\qquad$
$22 \quad A B C$ and $A C D$ are triangles.
$k$ is a constant.


22 (a) Show that $\overrightarrow{C D}=6 \mathbf{a}+4.5 \mathbf{b}$
[1 mark]
$\qquad$
$\qquad$
$\qquad$

22 (b) $B C D$ is a straight line.
Work out the value of $k$.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

23 | Simplify $\quad 8^{4} \div 32^{\frac{2}{5}}$ |
| :--- |
| Give your answer in the form $\quad 2^{m} \quad$ where $m$ is an integer. |
|  |

Answer $\qquad$
$24 \mathrm{f}(x)=\sin \left(x-90^{\circ}\right)$
Circle the value of $f\left(0^{\circ}\right)$
[1 mark]
$1 \quad 0 \quad-\frac{1}{2} \quad-1$

Turn over for the next question
$25 \quad P(4,8)$ is a point on a circle, centre $O$.
The tangent at $P$ intersects the axes at points $A$ and $B$.


25 (a) Show that the gradient of the tangent is $-\frac{1}{2}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

25 (b) Work out the length $A B$.
Give your answer in the form $a \sqrt{5}$ where $a$ is an integer.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ units

## Turn over for the next question

26 The turning point of the graph $y=(x+a)^{2}+b$ has $x$-coordinate -2 $(3,1)$ is another point on the graph.

Work out the $y$-coordinate of the turning point.

Answer $\qquad$

27 Angle $x$ is acute.

$$
\cos x=\sin 60^{\circ} \times \tan 30^{\circ}
$$

Work out the size of angle $x$.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ degrees

## END OF QUESTIONS



